



5.00 credits

30.0 h + 15.0 h

Q1

Teacher(s)	Vitale Enrico ;
Language :	French
Place of the course	Louvain-la-Neuve
Prerequisites	<p>Cours LMAT1131.</p> <p>Topics discussed in the course :</p> <p>solution of systems of algebraic equations.</p> <p>Arithmetic of polynomial rings and elimination theory.</p> <p>Structure of modules over a principal ideal domain, and application to the classification of linear operators on finite-dimensional vector spaces.</p>
Main themes	<p>Solution of systems of algebraic equations.</p> <p>Arithmetic of polynomial rings and elimination theory.</p> <p>Structure of modules over a principal ideal domain, and application to the classification of linear operators on finite-dimensional vector spaces.</p>
Learning outcomes	<p>At the end of this learning unit, the student is able to :</p> <p>Contribution of the course to learning outcomes in the Bachelor in Mathematics programme.</p> <p>By the end of this activity, students will have made progress in :</p> <ul style="list-style-type: none"> - Recognising and understanding a basic foundation of mathematics. -- Choosing and using the basic tools of calculation to solve mathematical problems. -- Recognising the fundamental concepts of important current mathematical theories. -- Establishing the main connections between these theories, analysing them and explaining them through the use of examples. - Identifying, by use of the abstract and experimental approach specific to the exact sciences, the unifying features of different situations and experiments in mathematics or in closely related fields (probability and statistics, physics, computing). - Showing evidence of abstract thinking and of a critical spirit : <p>1 -- Arguing within the context of the axiomatic method, recognising the key arguments and the structure of a proof, constructing and drawing up a proof independently.</p> <p>-- Evaluating the rigour of a mathematical or logical argument and identifying any possible flaws in it.</p> <p>-- Distinguishing between the intuition and the validity of a result and the different levels of rigorous understanding of this same result.</p> <p>Learning outcomes specific to the course. By the end of this activity, students will be able to :</p> <ul style="list-style-type: none"> - Factor multivariate polynomials into irreducible factors. - Analyse systems of algebraic equations to determine whether they admit solutions and to represent them geometrically. - Find equations with a given parametrised set of solutions. - Analyse the structure of modules over a principal ideal domain. - Reduce linear operators over a finite-dimensional vector space to canonical forms.
Evaluation methods	<p>The assessment aims to test knowledge and understanding of concepts, examples and fundamental results, the ability to build a coherent reasoning, mastery of demonstration techniques introduced during the course. The assessment consists of a final oral exam. To establish the final grade, we will take into account the oral exam and active participation in the practical work.</p>
Teaching methods	<p>Learning activities consist of lectures including supervised exercise sessions. The lectures aim to introduce fundamental concepts, to explain them by showing examples and by delineating their use, to show their reciprocal connections and their connections with other courses in the programme for the Bachelor in Mathematics.</p> <p>The supervised exercise sessions aim to teach how to select the appropriate method in the resolution of exercises. The two activities are given in presential sessions.</p>
Content	<p>This course introduces abstract algebraic notions playing an important role throughout the cursus of Bachelor and Master in Mathematics : commutative rings and modules.</p> <p>The following topics are discussed :</p>

	<ul style="list-style-type: none"> - Commutative rings and ideals, quotient rings, isomorphism theorems, chinese remainder theorem. - Integral domains, local rings, localisations, fields of fractions. - Maximal ideals and Krull's theorem. - Polynomial rings. Euclidean rings, unique factorization domains (UFD). The ring of Gaussian integers. - Gauss' theorem : if A is a UFD, then the polynomial ring $A[X]$ is UFD. - Noetherian rings, Hilbert's basis theorem. - (Time permetting) Modules, direct sums and direct products, free modules and projectives, modules of finite type. - (Time permetting) Exact sequences, tensor products.
Inline resources	The syllabus, also including the exercise statements for the practicals, will gradually be made available on the course's MoodleUCLouvain site.
Bibliography	<p>Saunders MacLane & Garrett Birkhoff, Algebra, third edition, AMS Chelsea Publishing 1988</p> <p>Hymann Bass, Algebraic K-theory, W.A. Benjamin Inc. 1968</p>
Faculty or entity in charge	MATH

Programmes containing this learning unit (UE)				
Program title	Acronym	Credits	Prerequisite	Learning outcomes
Additionnal module in Mathematics	APPMATH	5		
Minor in Mathematics	MINMATH	4		
Bachelor in Mathematics	MATH1BA	5		